Name: \_

Circle True or False or leave blank. (1 point for correct answer, -1 for incorrect answer, 0 if left blank)

- 1. True False If we want to show that the statements  $S_n$  are true for all  $n \ge 0$ , we need to prove the base case n = 1.
- 2. True False When  $A \subset B$ , the conditional probability P(A|B) can be expressed as the fraction  $\frac{P(A)}{P(B)}$  (given all involved quantities are well-defined).

Show your work and justify your answers. Please circle or box your final answer.

3. (10 points) (a) (4 points) Prove that  $1 + 2 + \dots + n = \frac{n(n+1)}{2}$  for all  $n \ge 1$ .

(b) (3 points) What is the probability that when picking a hand of 5 cards out of a deck of 52 cards, you pick at least one king?

(c) (3 points) What is the probability that when picking a hand of 5 cards out of a deck of 52 cards, you pick exactly three kings given that you have at least one king?